

Nauta JJ, Beyer WE, Osterhaus AD.  
*On the relationship between mean  
antibody level, seroprotection and  
clinical protection from influenza.*

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Slides: <https://wzbillings.com/presentations/IDIG-2022-10-25/>

(this is a stock image that I got from powerpoint and Powerpoint said I am allowed to use it)



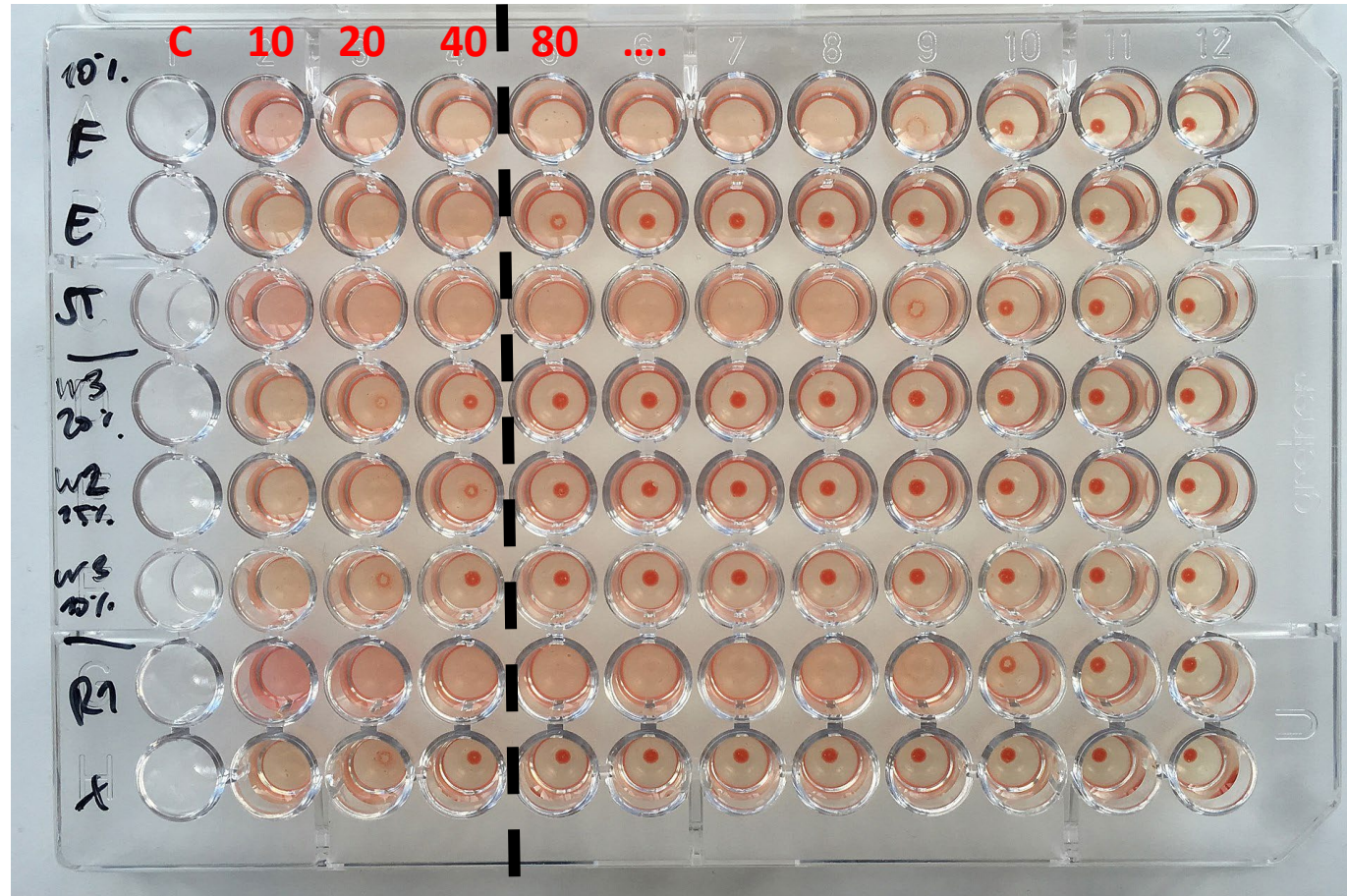
# Citation

- Nauta JJ, Beyer WE, Osterhaus AD. On the relationship between mean antibody level, seroprotection and clinical protection from influenza. *Biologicals*. 2009;37(4):216-221.  
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# Definitions (general)

- **CoP** (correlate of protection): an immunological measurement that is statistically associated with clinical protection from a condition.
- **Seroprotection**: having a serological measurement higher than some predetermined titer (usually the titer determined to be associated with 50% clinical protection).
- **Seroconversion**: an individual's serological measurement is lower than the threshold before an intervention, but is above the threshold after the intervention. (Protection + the intervention did it.)
- **Clinical protection**: reduced risk for an individual to acquire a condition.

# HAI and the magical 1:40 titer



# Background/motivation

- HAI is a CoP for flu
- We can therefore use it to measure vaccine efficacy
- How do mean HAI titer, seroprotection, and clinical protection relate?  
All of these are commonly used.
- **Main question:** does a higher mean titer or seroprotection risk always reflect an increase in clinical protection?

The model

$$t = \log_2 (\text{HAI titer}/5)$$

$$t \sim \text{Normal}(\mu, \sigma)$$

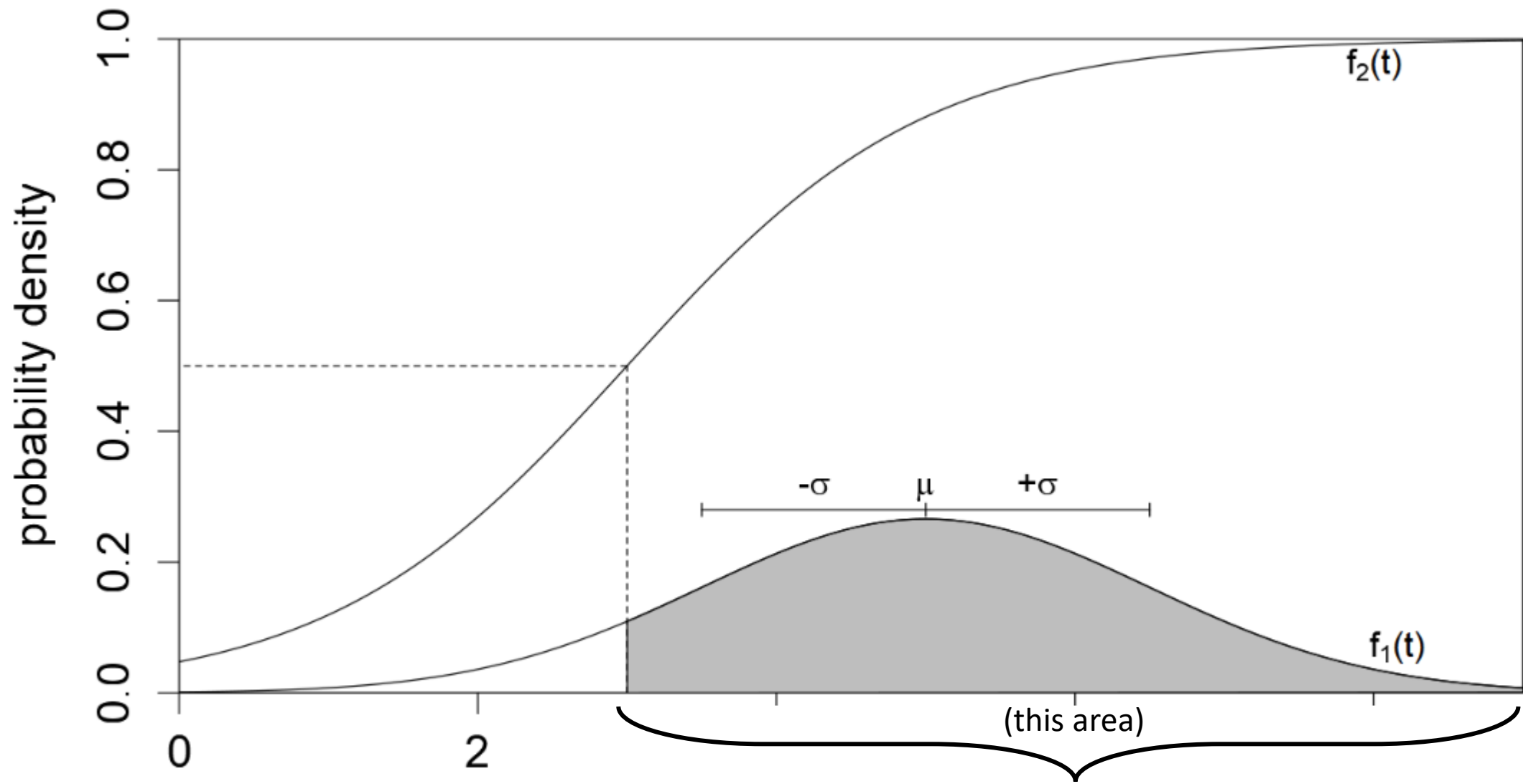
$$\pi_{\text{seroprotection}} = \int_{t_p}^{\infty} f(t) dt$$

$$\pi_{\text{clinical protection}} = \int_{-\infty}^{\infty} f(t) \frac{\lambda}{(1 + \exp(\alpha + \beta t))} dt$$

$$0 < \lambda \leq 1, \alpha > 0, \beta < 0$$



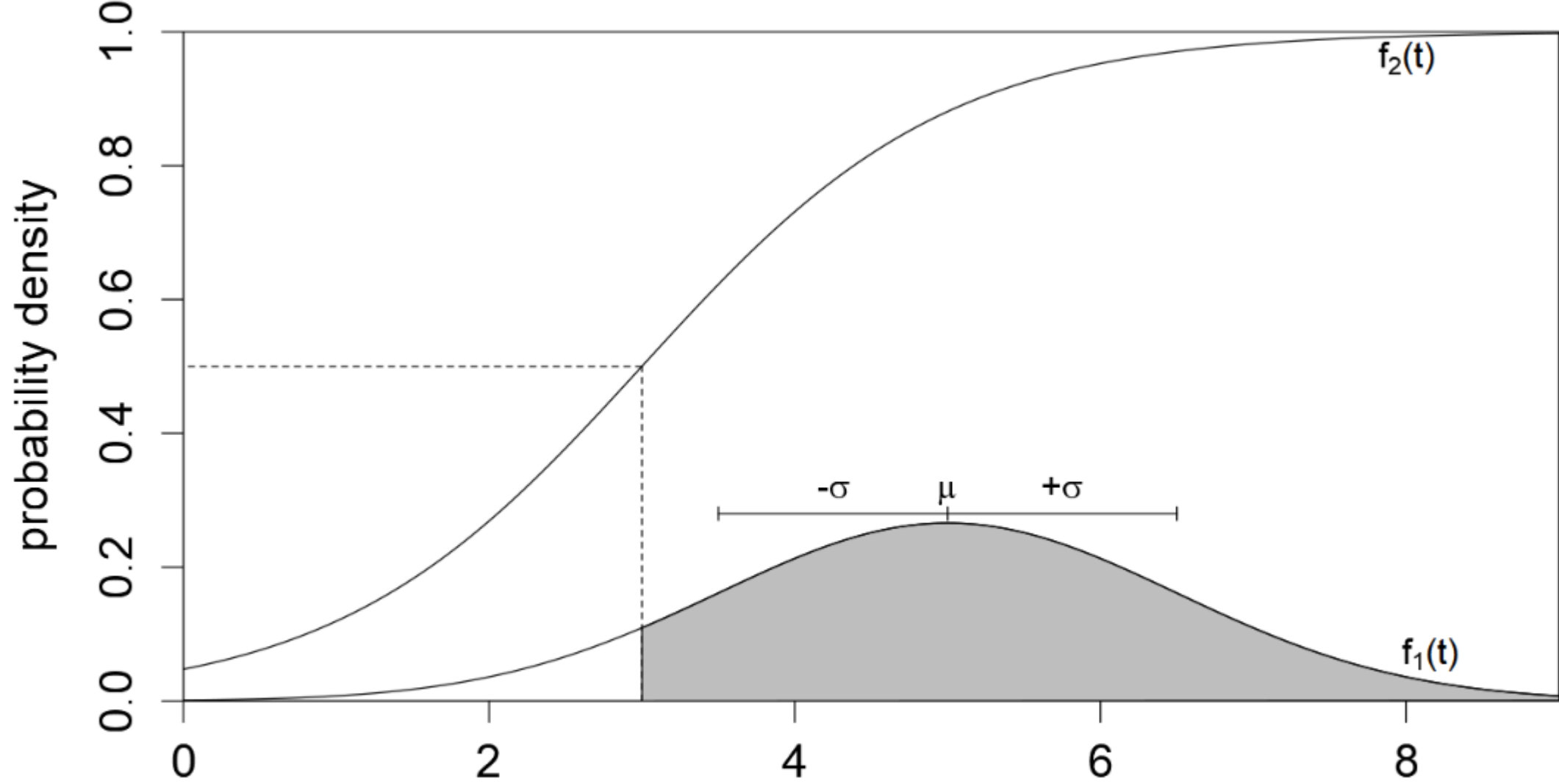
- $\lambda$  is the probability of clinical protection for subjects with "a very high HI titer".
- $\alpha$  accounts for protection unrelated to antibody level.
- $\beta$  is the slope of the clinical protection curve.



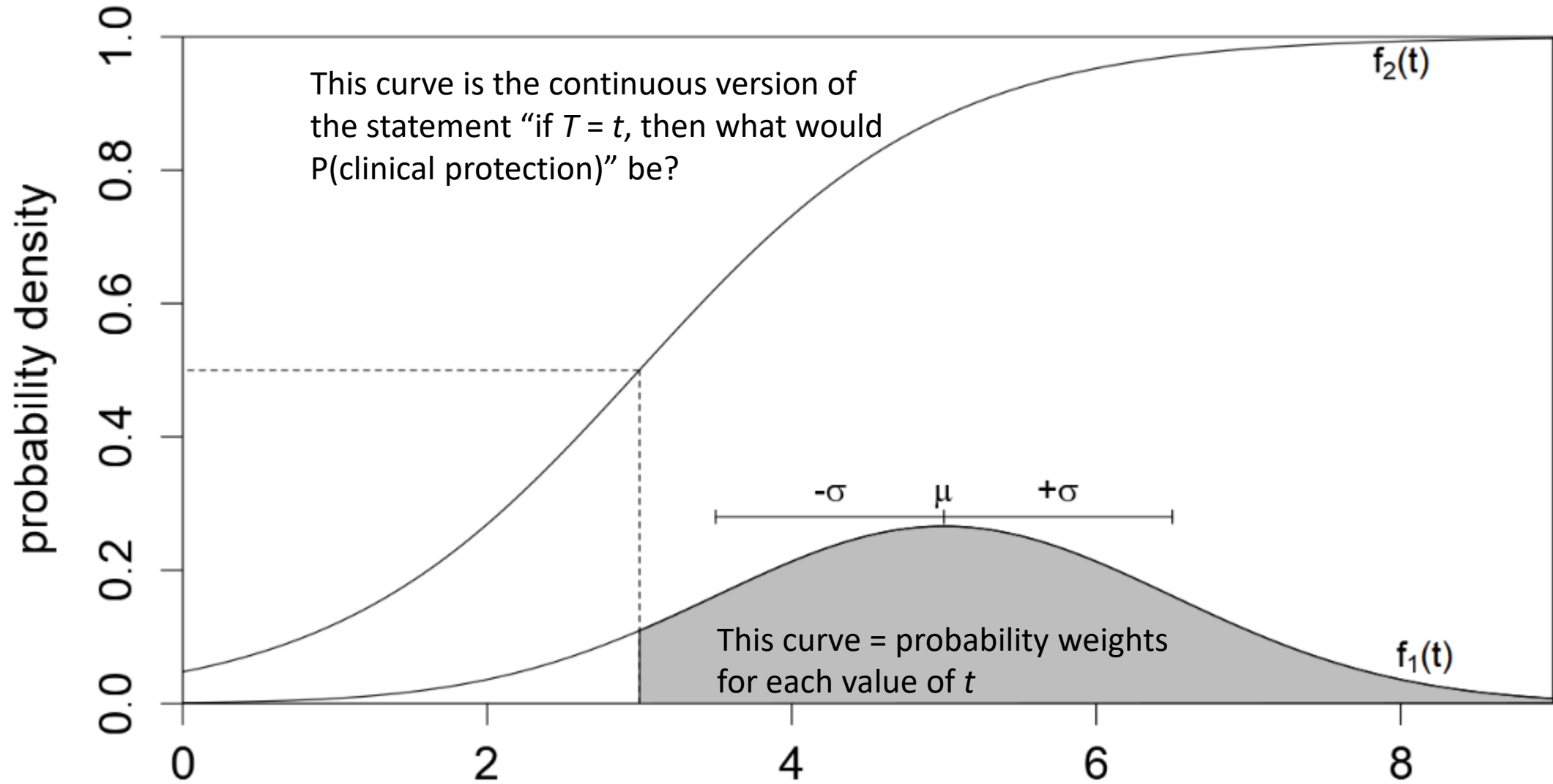
$P(\text{seroprotected})$  is just the calculated probability from the normal model.
 
$$P(t \geq 3) = \int_3^{\infty} f_1(t) dt$$

P(clinical protection) is defined (by the authors) as the expected value of  $f_2$ .

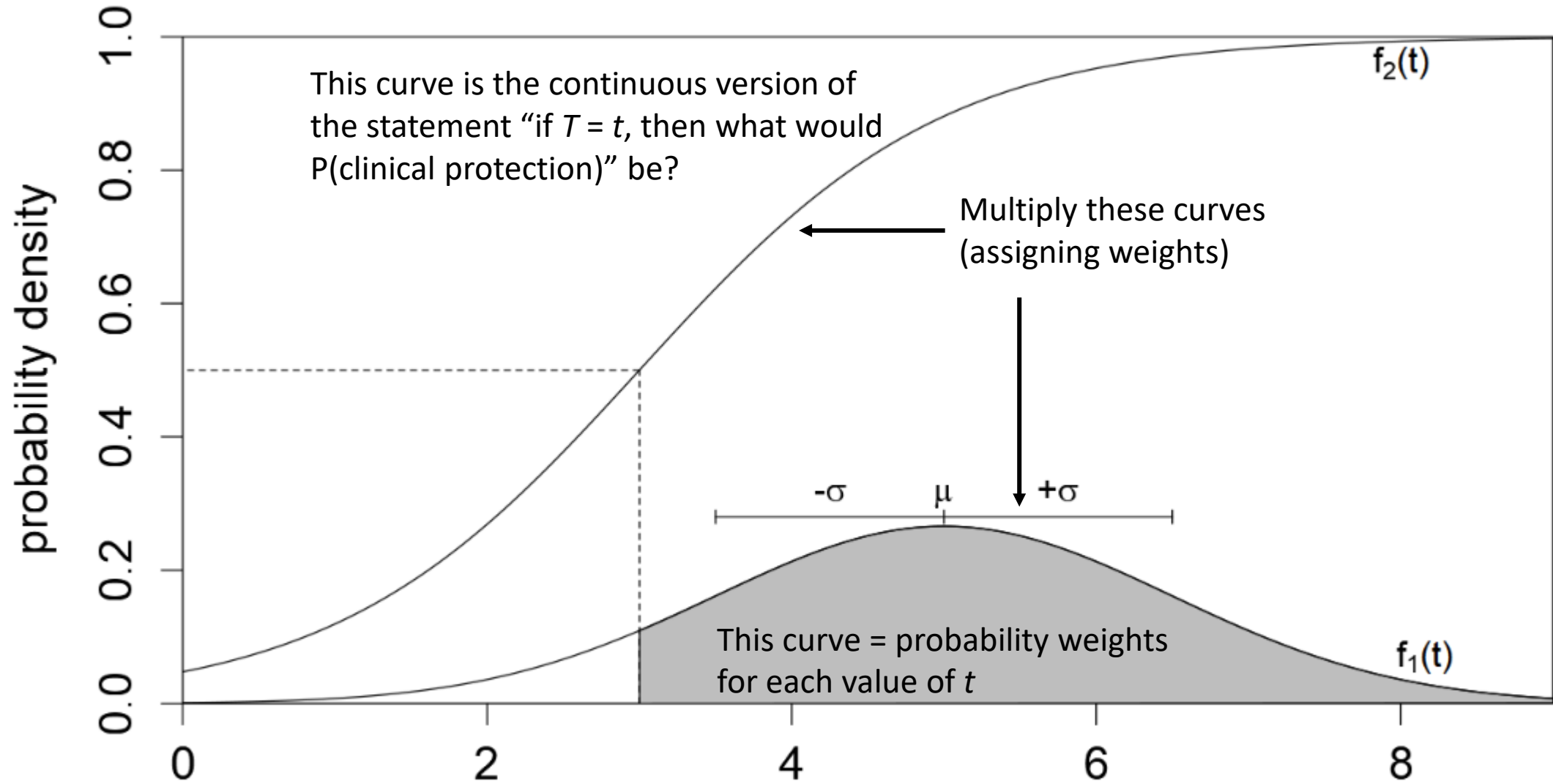
Essentially asking the question, "What is the average value of P(clinical protection) in our model?"



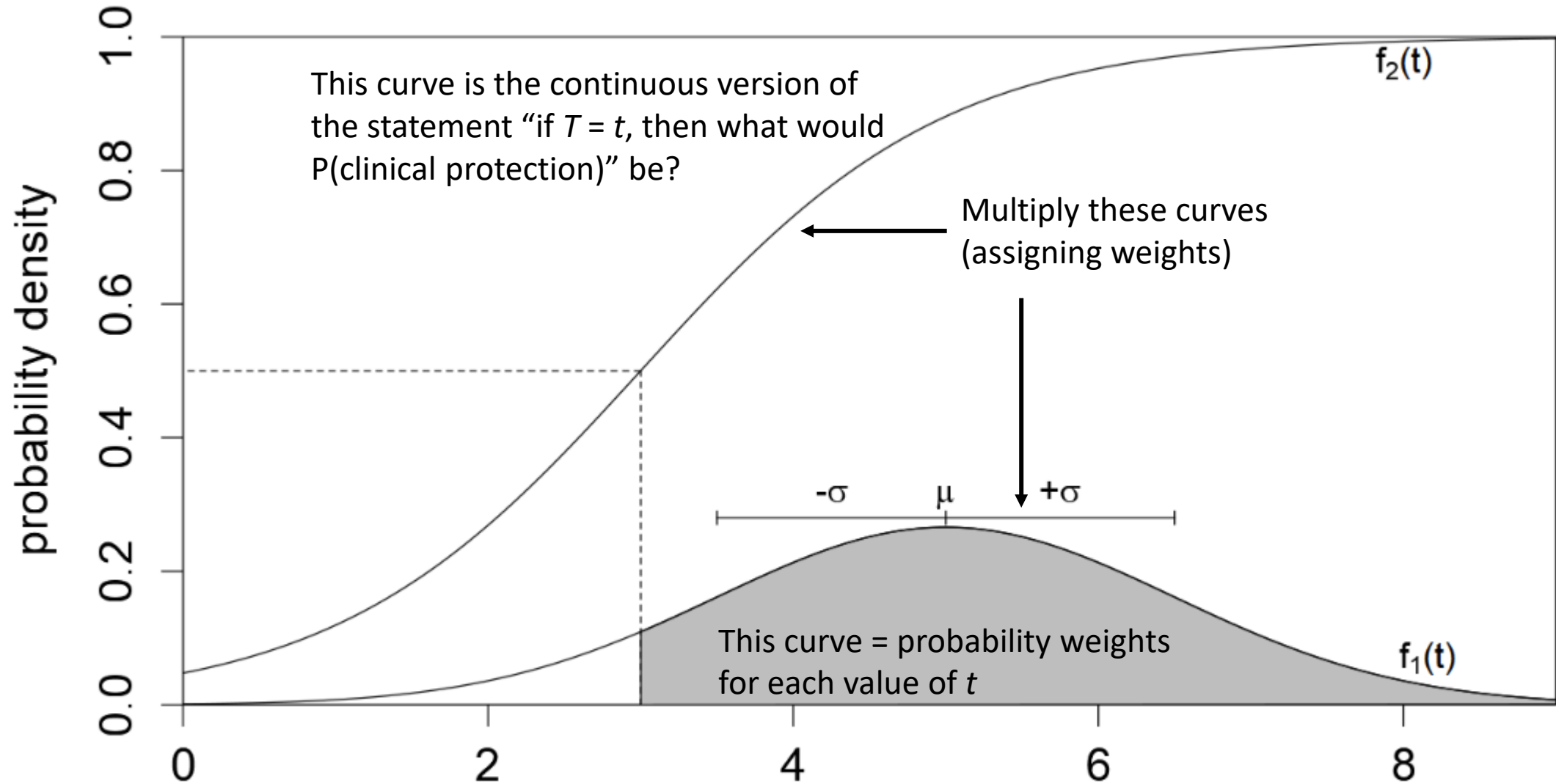
P(clinical protection) is defined (by the authors) as the expected value of  $f_2$



$P(\text{seroconverted})$  is defined (by the authors) as the expected value of  $f_2$



P(seroconverted) is defined (by the authors) as the expected value of  $f_2$



Then integrate (continuous version of a weighted sum)! So,  $P(\text{protected}) = E[f_2(t)] = \int_{-\infty}^{\infty} f_1(t) f_2(t) dt$

# Other thoughts about the model

- If all  $t$  were equally likely, we could just use the sample mean of  $f_2(t)$ .
- If one is willing to specify  $t_p, \alpha, \lambda$ , then we get

$$\beta = \frac{\log(2\lambda - 1) - \alpha}{t_p}.$$

- CIs are pretty easy but they don't mention them.

anyways.



# Results

- For the record, Table 3 is pretty much useless to me. As Richard McElreath says, “you can stare at a table, and it will stare back.”
- Figure 2:
  - Higher alpha = steeper slope? (We aren't holding beta constant)
  - Lambda is a threshold for the max “allowed” protection probability.
  - They don't identify which curve has which  $t_p$ . (rolling eyes emoji)

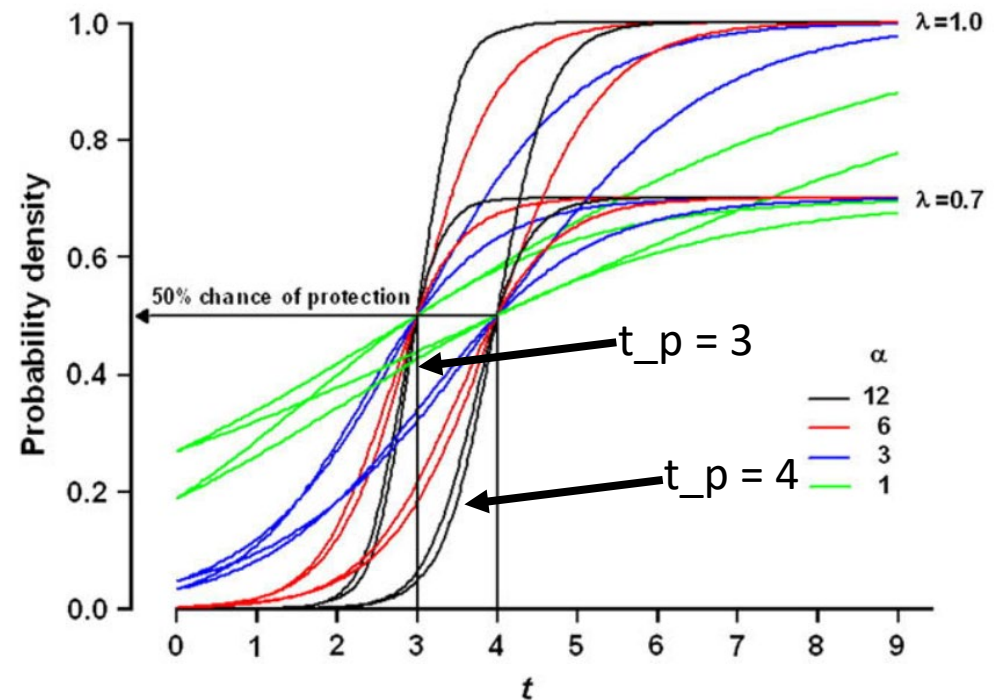


Fig. 2. Clinical protection curves examined in the statistical model.

# Results

- It really bugs me when published papers have incorrectly labeled graphs.
- But the important result here is that the risk of seroprotection varies with **both** the mean and variance of  $t$ .
- For clinical protection, the variance is more influential the larger alpha is (no plot, stare at the table until you realize this).

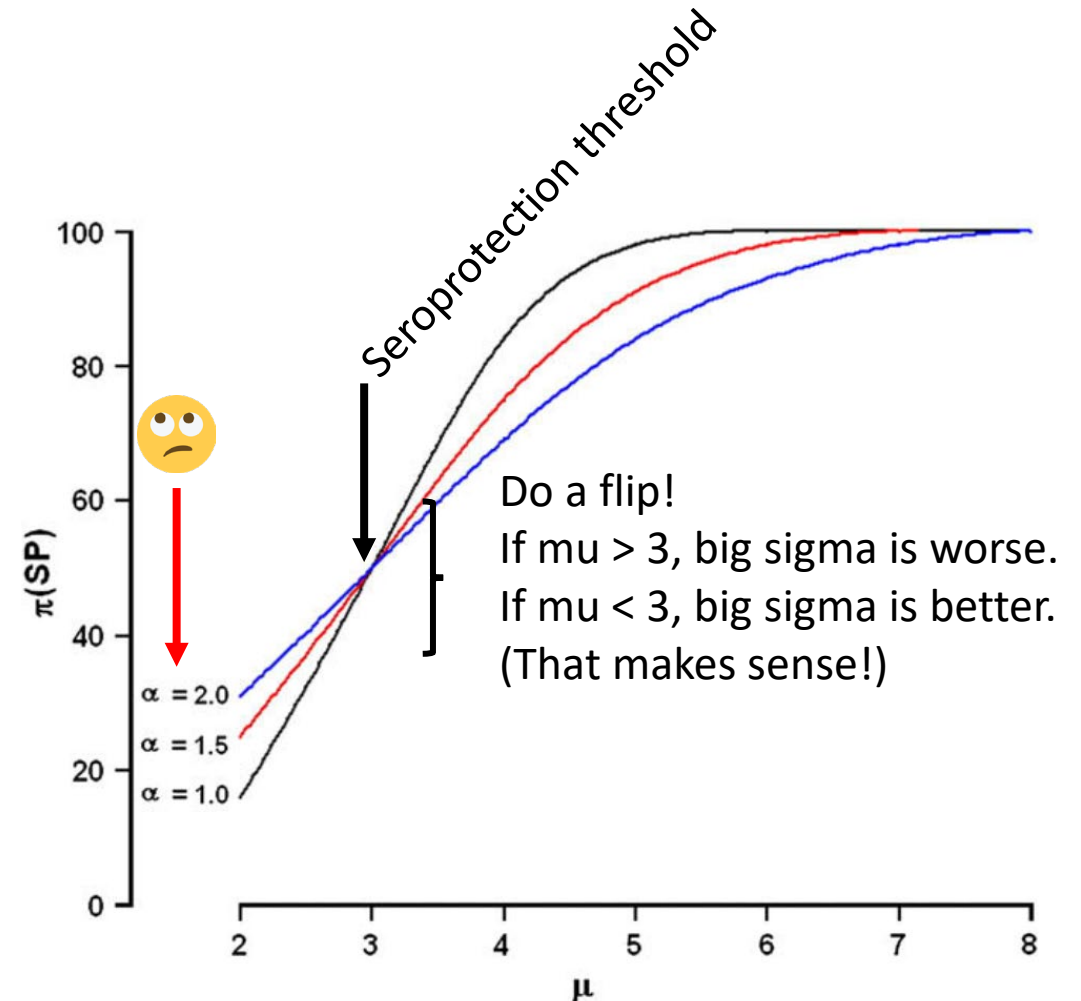


Fig. 3. Relationship between output parameter  $\pi(\text{SP})$  and input parameters  $\mu$  and  $\sigma$ .

# So what?

- This makes a difference in interpreting mean titer values between two groups during a trial. The rules they provide are pretty interesting to read through. I've never seen anyone use them though.
- **Main conclusion: it is misleading to interpret differences in mean titer, seroprotection, or clinical protection without considering both the mean and variance of the titers.**

# So what part 2: the mystery of the magical 1:40 titer continues

- Secondary conclusion: clinical protection levels depend on parameters for which they provide no data-based estimates. Maybe this has already been done, I haven't checked. If not, flu surveillance datasets do exist and this could be interesting.
- It would also be easy to do a much more in-depth simulation/modeling study than they did here.
- **HOWEVER**, their conclusions are explicitly based on the  $t = 3$  (i.e. magical 1:40) threshold. Where does it come from, is it strain-specific, and is it even valid?